# CS 61A Spring 2023

# Structure and Interpretation of Computer Programs

FINAL SOLUTIONS

#### INSTRUCTIONS

This is your exam. Complete it either at exam.cs61a.org or, if that doesn't work, by emailing course staff with your solutions before the exam deadline.

This exam is intended for the student with email address <EMAILADDRESS>. If this is not your email address, notify course staff immediately, as each exam is different. Do not distribute this exam PDF even after the exam ends, as some students may be taking the exam in a different time zone.

For questions with **circular bubbles**, you should select exactly *one* choice.

You must choose either this option
Or this one, but not both!

For questions with **square checkboxes**, you may select multiple choices.

You could select this choice.

You could select this one too!

You may start your exam now. Your exam is due at <DEADLINE> Pacific Time. Go to the next page to begin.

# Preliminaries

(a)	What is your full name?		
(b)	What is your student ID number?		

You can complete and submit these questions before the exam starts.

(c)	What is your @berkeley.edu email address?

` '	Sign (or type) your name to confirm that all work on this exam will be your own. The penalty misconduct on an exam is an F in the course.	for academic

## 1. (10.0 points) What Would Python Display?

Assume the following code has been executed. The Link class appears on the midterm 2 study guide.

```
class Chain(Link):
    def add(self, v):
        self.rest = Chain(v, self.rest)
        return self

gold = Chain(3, Chain(5, Chain(7)))

silver = [1, [2], 3]
bronze = silver[1:]
silver.append(4)
silver[1].append(5)
```

For each expression below, choose the output displayed when the expression is evaluated. Assume the expressions are evaluated in order in the same interactive session, and so evaluating an earlier expression may affect the result of a later one.

```
(a) (3.0 pt) print(gold.rest.add(1))
```

- <3 1 5 7>
- <3 <1> 5 7>
- <3 5 1 7>
- <3 5 <1> 7>
- <5 1 7>
- O <5 <1> 7>
- O None of these

#### (b) (3.0 pt) print(Chain(2, gold).add(4))

```
<2 4 3 5 1 7>
```

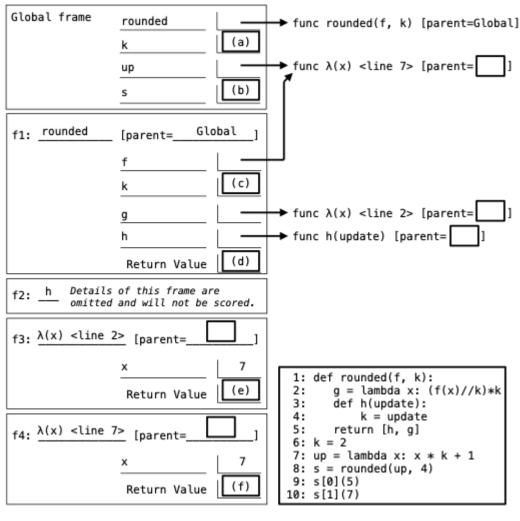
(c) (2.0 pt) print(bronze)

```
[[2, 5], 3]
```

- (d) (2.0 pt) What is the order of growth of the time to run the Chain.add method with respect to the length of self?
  - Constant
  - Logarithmic
  - O Linear
  - O Quadratic
  - Exponential

#### 2. (5.0 points) Framed

Complete the environment diagram that results from running all of the code below and then answer the questions that follow. Blanks with no labels have no questions associated with them and are not scored.



- (a) (1.0 pt) Fill in blank (a).
  - **2**
  - $\bigcirc$  4
  - $\bigcirc$  5
  - O None of these
- (b) (1.0 pt) Blanks (b) and (d) have the same value; what is it?
  - O Two functions
  - A list containing two functions
  - A list containing a list of two functions
  - A list containing two lists that each contain one function

- (c) (3.0 pt) What three numbers fill in blanks (c), (e), and (f) respectively?
  - 4, 12, 15
  - $\bigcirc$  4, 14, 15
  - $\bigcirc$  4, 15, 15
  - $\bigcirc$  4, 25, 29
  - $\bigcirc$  4, 28, 29
  - $\bigcirc$  4, 36, 36
  - $\bigcirc$  5, 12, 15
  - $\bigcirc\ 5,\,15,\,15$
  - $\bigcirc$  5, 25, 29
  - $\bigcirc$  5, 28, 29
  - $\bigcirc$  5, 36, 36

## 3. (16.0 points) Trees Get Degrees

s.label > t.label

## (a) (10.0 points)

Implement big\_paths, which takes a Tree instance t with number labels. It returns the number of paths from the root of t to a leaf in which all labels are greater than or equal to the root label. The Tree class appears on the midterm 2 study guide.

```
def big_paths(t):
    """Return the number of paths from the root to a leaf in which all labels are
   greater than or equal to the root label of t.
   >>> t = Tree(5, [Tree(4, [Tree(6), Tree(7)]), Tree(8), Tree(7, [Tree(5), Tree(3)])])
   >>> big_paths(t) # 5-8 and 5-7-5
   2
   11 11 11
   def f(s):
       if ____:
            (a)
           return 0
       elif ____:
               (b)
           return 1
        else:
           return _____
                    (c)
   return _____
             (d)
 i. (2.0 pt) Fill in blank (a).
       s.is_leaf()
    t.is_leaf()
   t.label >= s.label
    s.label >= t.label
   t.label > s.label
    s.label > t.label
ii. (2.0 pt) Fill in blank (b).
   s.is_leaf()
       t.is_leaf()
   t.label >= s.label
    s.label >= t.label
    t.label > s.label
```

iii. (4.0 pt) Fill in blank (c).

```
sum([f(b) for b in s.branches])
```

- iv. (2.0 pt) Fill in blank (d).
  - (s)
  - f(t)
  - O f(s, 0)
  - O f(t, 0)
  - $\bigcirc$  1 + f(s, 0)
  - $\bigcirc$  1 + f(t, 0)

gen(b, n)

## (b) (6.0 points)

```
Implement gen, a generator function that takes a Tree instance t with number labels and a number n. It yields a two-element list for every pair of a parent label and child label that sum to n.
```

```
def gen(t, n):
    """Yield all pairs of a parent label and child label that sum to n in tree t.
   >>> t = Tree(5, [Tree(4, [Tree(6), Tree(7)]), Tree(8), Tree(7, [Tree(5), Tree(3)])])
   >>> sorted(gen(t, 10)) # Does not yield [5, 5]; one 5 is the grandparent of the other.
    [[4, 6], [7, 3]]
    11 11 11
   for b in ____:
               (e)
        if ____ == n:
             (f)
               (g)
        yield from ____
                      (h)
 i. (1.0 pt) Fill in blank (e).
   t.branches
   gen(t.branches, n)
   map(lambda x: gen(x, n), t.branches)
ii. (1.0 pt) Fill in blank (f).
   O b.label
   ① t.label
   t.label + b.label
    sum([b.label for b in t.branches])
iii. (2.0 pt) Fill in blank (g).
      yield [t.label, b.label]
iv. (2.0 pt) Fill in blank (h).
    t.branches
   O b.branches
   [[t, b] for b in t.branches]
   [[t.label, b.label] for b in t.branches]
   \bigcirc gen(t, n)
```

## 4. (6.0 points) Repark the Car

**Definition.** A car takes up 2 adjacent parking spots. A string of length n can represent n adjacent parking spots using <> for a car and . for an empty spot. For example '.<>.<><' represents an empty spot, then two spots containing a car, then another empty spot, then four spots containing two cars.

Implement cars, which takes non-negative integers k and n. It returns the number of ways to park k cars in n adjacent parking spots. Treat all cars the same; it does not matter which car is parked in which spot.

```
def cars(k, n):
    """Return the number of ways to park k cars in n adjacent parking spaces where
    each car takes up two spaces.
    >>> cars(2, 5) # '<><>.', '<>.<>', '.<><>'
    >>> cars(3, 6) # '<><>'
    >>> cars(1, 7) # '<>....', '.<>....', etc.
    11 11 11
    if k == 0:
        return _____
                   (a)
    if ____:
          (b)
        return 0
    return _____
               (c)
(a) (1.0 pt) Fill in blank (a).
    \bigcirc 0
     1
    \bigcirc n
    On + 1
(b) (2.0 pt) Fill in blank (b).
    \bigcirc k > 0
    ○ k < 0</p>
    \bigcirc n == 0
    O n < 1
```

(c) (3.0 pt) Fill in blank (c).

n < 2

```
cars(k, n-1) + cars(k-1, n-2)
```

## 5. (16.0 points) Pairings

**Definition.** The *pairing* of a sequence **s** is a sequence of pairs containing all of the elements of **s** in order. A pair is a two-element list. E.g., the pairing of [1, 3, 5, 6, 4, 2] is [[1, 3], [5, 6], [4, 2]].

(a) (6.0 points)

```
Implement pair, a function that takes a list s with an even length. It returns the pairing of s.
```

def pair(s):

"""Return the pairing of an even-length list s as a list of two-element lists.

```
>>> pair([3, 4, 5, 8, 7, 6])
[[3, 4], [5, 8], [7, 6]]
"""
assert len(s) % 2 == 0
return [______ for i in _____]
(a) (b)
```

i. (3.0 pt) Fill in blank (a).

```
[s[2 * i], s[2 * i + 1]] OR s[2*i:2*i+2]
```

- ii. (1.0 pt) Fill in blank (b). The built-in map function appears on the midterm 2 study guide.
  - $\bigcirc$  map(lambda x: x // 2, s)
  - $\bigcirc$  map(lambda x: s // 2, s)
  - range(len(s // 2))
  - range(len(s) // 2)
- iii. (2.0 pt) Fill in blank (c) in the implementation of gen\_pairs, a generator function that takes an infinite iterator t. It yields the elements of the pairing of the sequence represented by t.

```
[next(t), next(t)]
```

(b)	(10.0	points)
-----	-------	---------

(10.0	pomes)
	ement pairs, a Scheme procedure that takes a list s with an even length. It returns the pairing of s. xample, (pairs '(3 4 5 8 7 6)) evaluates to ((3 4) (5 8) (7 6)).
(def:	ine (pairs s) (if (null? s) nil ( ( list (car s) ) )))  (d) (e) (f)
i. (	<b>1.0 pt)</b> Fill in blank (d).
(	) append
(	car
(	○ cdr
	cons
(	) if
(	list
ii. (	(2.0 pt) Fill in blank (e).
	(car (cdr s))
iii. (	(2.0 pt) Fill in blank (f).
	(pairs (cdr (cdr s)))
,	(2.0 pt) What is the value of the expression (map pairs (pairs '(3 4 5 6)))? The built-in map procedure appears on the final study guide. Assume pairs is implemented correctly.
(	(3 4 5 6)
(	((3 4) (5 6))
(	(((3 4) (5 6)))
(	((3 (4)) (5 (6)))
	(((3 4)) ((5 6)))
`	(3.0 pt) Which expressions are passed to scheme_eval when evaluating ((lambda (x) 1) 2)? Check all that apply.
	((lambda (x) 1) 2)
	(lambda (x) 1)
	□ lambda
	□ (x)
	□ x
	1

# 6. (14.0 points) Log and Count

## (a) (6.0 points)

The Log class is constructed with a one-argument function f and has a method call that takes n and returns f(n). The args attribute of a Log instance for function f is a list containing all n passed to the call method of any Log instance with the same f.

class Log:

"""Store the arguments passed to a one-argument function in a list called args. If two logs are created for the same function f, they share a list of args.

```
>>> f = Log(lambda x: x * x)
>>> f.call(f.call(3))
81
>>> f.args
[3, 9]
>>> g, h = Log(abs), Log(abs)
>>> g.call(h.call(-3))
>>> g.args
[-3, 3]
11 11 11
logged = {}
def __init__(self, f):
    if f not in self.logged:
        ____ = []
           (a)
    self.f = _____
                (b)
    self.args = _____
                   (c)
def call(self, n):
    self.args.append(n)
    return _____
              (d)
```

i. (3.0 pt) One expression can fill both blanks (a) and (c); what is it?

```
self.logged[f] or Log.logged[f]
```

ii. (1.0 pt) Fill in blank (b).

```
f
```

- iii. (2.0 pt) Fill in blank (d).
  - Log.call(self, n)
  - self.call(n)
  - self.f(n)
  - self.f.call(n)

# (b) (8.0 points)

The Counter class has a method observe that takes an iterable and a method count that takes a value v and returns the number of times v appears among the elements of all the iterables ever passed to observe. Finally, the forget method takes no arguments and omits the values of the most recent (not yet forgotten) call to observe from subsequent calls to count. Assume forget is never called more times than observe.

Hint: The built-in count method of a list returns the count of a value: [3, 4, 3].count(3) is 2.

#### class Counter:

"""Counts the number of times a value was observed.

```
>>> c = Counter()
>>> c.observe(map(abs, range(-3, 3))) # observe 3, 2, 1, 0, 1, 2
>>> c.observe(range(-3, 3))
                                        # observe -3, -2, -1, 0, 1, 2
>>> {i: c.count(i) for i in range(-3, 3)}
\{-3: 1, -2: 1, -1: 1, 0: 2, 1: 3, 2: 3\}
>>> c.forget() # forget range(-3, 3)
>>> {i: c.count(i) for i in range(-3, 3)}
\{-3: 0, -2: 0, -1: 0, 0: 1, 1: 2, 2: 2\}
>>> c.forget() # forget map(abs, range(-3, 3))
>>> c.count(1)
0
11 11 11
def __init__(self):
    self.obs = []
def observe(self, vs):
       (e)
def count(self, v):
    return _____
              (f)
def forget(self):
       (g)
```

i. (3.0 pt) Fill in blank (e).

```
self.obs.append(list(vs))
```

**ii.** (3.0 pt) Fill in blank (f).

```
sum([s.count(v) for s in self.obs])
```

iii. (2.0 pt) Fill in blank (g).

```
Obs.pop()
```

```
self.obs.pop()
```

- O [obs.pop() for i in range(len(vs))]
- [self.obs.pop() for i in range(len(vs))]

#### 7. (8.0 points) Room Service

The finals table has columns hall (strings) and course (strings), and has rows for each lecture hall in which a course is holding its final exam. Each course and each hall value may appear multiple times because a course may use multiple lecture halls at the same time, and a lecture hall may hold finals for multiple courses at different times.

The sizes table has columns room (strings) and seats (numbers), and has one row per unique room on campus containing the number of seats in that room. Each room appears once. All lecture halls are rooms.

Create a table with two columns, course (string) and seats (number), and with one row containing the name of the course and the total number of seats in final rooms for that course. Only include a row for each course that uses at least two rooms for its final.

finals:	hall	course
	RSF	61A
	Wheeler	61A
	RSF	61B

:	room	seats
	RSF	900
	Wheeler	700
	310 Soda	40

result: c	ourse	seats
6	51A	1600

SELECT course, SUM(\_\_\_\_\_\_) AS seats FROM \_\_\_\_\_\_ GROUP BY \_\_\_\_\_\_;
(a) (b) (c)

- (a) (1.0 pt) Fill in blank (a).
  - O course
  - $\bigcirc$  room
  - seats
  - sizes
- (b) (4.0 pt) Fill in blank (b). You may include a WHERE or HAVING clause.

finals, sizes WHERE hall=room

- (c) (3.0 pt) Fill in blank (c).
  - O hall WHERE seats > 1
  - hall HAVING seats > 1
  - hall WHERE sizes > 1
  - hall HAVING sizes > 1
  - hall WHERE COUNT(\*) > 1
  - hall HAVING COUNT(\*) > 1
  - course WHERE seats > 1
  - course HAVING seats > 1
  - O course WHERE sizes > 1
  - O course HAVING sizes > 1
  - Course WHERE COUNT(\*) > 1
  - course HAVING COUNT(\*) > 1

#### 8. Group Work

These A+ questions are not worth any points. They can only affect your course grade if you have a high A and might receive an A+. Finish the rest of the exam first!

**Definition.** The *n*-grouping of a list **s** for positive integer **n** is a list of **n**-length lists containing all of the elements of **s** in order. The last list may contain fewer than **n** elements.

```
E.g., the 3-grouping of [4, 3, 2, 1, 5, 6, 7, 8] is [[4, 3, 2], [1, 5, 6], [7, 8]].
```

(a) Fill in the blank to implement group, which takes positive integer n and list s. It returns the the n-grouping of s.

(b) Fill in the blank to implement group, which takes positive integer n and list s. It returns the the n-grouping of s.

No more questions.