CS 61A Structure and Interpretation of Computer Programs Fall 2020 MIDTERM 2

INSTRUCTIONS

This is your exam. Complete it either at exam.cs61a.org or, if that doesn't work, by emailing course staff with your solutions before the exam deadline.

This exam is intended for the student with email address <EMAILADDRESS>. If this is not your email address, notify course staff immediately, as each exam is different. Do not distribute this exam PDF even after the exam ends, as some students may be taking the exam in a different time zone.

For questions with circular bubbles, you should select exactly one choice.

- \bigcirc You must choose either this option
- \bigcirc Or this one, but not both!

For questions with square checkboxes, you may select *multiple* choices.

- \Box You could select this choice.
- \Box You could select this one too!

You may start your exam now. Your exam is due at *<*DEADLINE*>* Pacific Time. Go to the next page to begin.

Preliminaries

You can complete and submit these questions before the exam starts.

- (a) What is your full name?
- (b) What is your student ID number?

1. (8.0 points) Political Environment

Fill in each blank in the code example below so that executing it would generate the following environment diagram.

RESTRICTIONS. You must use all of the blanks. Each blank can only include one statement or expression. Click here to open the diagram in a new window/tab



- v(m, 5, 6)
- (a) (2.0 pt) Fill in blank (a). You may not write any numbers or arithmetic operators (+, -, *, /, //, **) in your solution.
- (b) (2.0 pt) Fill in blank (b). You may not write any numbers or arithmetic operators (+, -, *, /, //, **) in your solution.
- (c) (2.0 pt) Fill in blank (c). You may not write any numbers or arithmetic operators (+, -, *, /, //, **) in your solution.
- (d) (2.0 pt) Which of these could fill in blank (d)? Check all that apply.
 - □ o
 - [o]
 - list(o)
 - [list(o)]
 - list([o])
 - □ o + []
 - □ [o[0], o[1]]
 - □ o[:]

2. (10.0 points) Yield, Fibonacci!

(a) (4.0 points)

Implement fibs, a generator function that takes a one-argument pure function f and yields all Fibonacci numbers x for which f(x) returns a true value.

The Fibonacci numbers begin with 0 and then 1. Each subsequent Fibonacci number is the sum of the previous two. Yield the Fibonacci numbers in order.

```
def fibs(f):
```

```
"""Yield all Fibonacci numbers x for which f(x) is a true value.
  >>> odds = fibs(lambda x: x % 2 == 1)
  >>> [next(odds) for i in range(10)]
  [1, 1, 3, 5, 13, 21, 55, 89, 233, 377]
  >>> bigs = fibs(lambda x: x > 20)
  >>> [next(bigs) for i in range(10)]
  [21, 34, 55, 89, 144, 233, 377, 610, 987, 1597]
  >>> evens = fibs(lambda x: x % 2 == 0)
  >>> [next(evens) for i in range(10)]
  [0, 2, 8, 34, 144, 610, 2584, 10946, 46368, 196418]
  .....
  n, m = 0, 1
  while _____:
           (a)
       if ____:
            (b)
             _____
             (c)
       _____
         (d)
i. (1.0 pt) Which of these could fill in blank (a)?
```

- \bigcirc f(n)
- \bigcirc f(m)
- \bigcirc f(n) or f(m)
- \bigcirc f(n) and f(m)
- \bigcirc True
- False

- ii. (1.0 pt) Which of these could fill in blank (b)?
 - \bigcirc f(n)
 - \bigcirc f(m)
 - \bigcirc f(n) or f(m)
 - \bigcirc f(n) and f(m)
 - \bigcirc True
 - \bigcirc False
- **iii.** (1.0 pt) Fill in blank (c).

iv. (1.0 pt) Fill in blank (d).

(b) (6.0 points)

Definition. For a linked list s, the *index* of an element is the number of times **rest** appears in the smallest dot expression containing only s, **rest**, and **first** that evaluates to that element. For example, in the linked list s = Link(5, Link(7, Link(9, Link(11)))),

- The index of 5 (s.first) is 0.
- The index of 7 (s.rest.first) is 1.
- The index of 11 (s.rest.rest.rest.first) is 3.

Implement filter_index, a function that takes a one-argument pure function f and a Link instance s. It returns a Link containing all elements of s that have an index i for which f(i) returns a true value.

Assume that **s** is a finite linked list of numbers that contains no repeated elements. The Link class appears on Page 2 (left column) of the Midterm 2 Study Guide.

```
def filter_index(f, s):
    """Return a Link containing the elements of Link s that have an index i for
    which f(i) is a true value.
   >>> powers = Link(1, Link(2, Link(4, Link(8, Link(16, Link(32))))))
   >>> filter_index(lambda x: x < 4, powers)
   Link(1, Link(2, Link(4, Link(8))))
   >>> filter_index(lambda x: x % 2 == 1, powers)
   Link(2, Link(8, Link(32)))
    .....
   def helper(i, s):
        if s is Link.empty:
           return s
        filtered_rest = _____
                           (a)
        if ____:
              (b)
           return ____
                      (c)
        else:
            return filtered_rest
    return _____
             (d)
```

- i. (1.0 pt) Which of these could fill in blank (a)?
 - O helper(i + 1, s.rest)
 - O helper(i + 1, s.rest.rest)
 - filter_index(f, s.rest)
 - filter_index(f, s.rest.rest)
 - O Link(helper(i + 1, s.rest))
 - O Link(helper(i + 1, s.rest.rest))
 - O Link(filter_index(f, s.rest))
 - O Link(filter_index(f, s.rest.rest))
- **ii.** (1.0 pt) Fill in blank (b).
- **iii.** (2.0 pt) Fill in blank (c).
- iv. (2.0 pt) Fill in blank (d).

3. (12.0 points) Sparse Lists

The most_common function returns the most common element in a non-empty list. You do not need to implement this function. Assume that it is implemented for you.

```
def most_common(s):
    """Return the most common element in non-empty list s. In case of a tie,
    return the most common element that appears first in s.
    >>> most_common([3, 1, 4, 1, 5, 9])
    1
    >>> most_common([3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5])
    5
    >>> most_common([2, 7, 1, 8, 2, 8, 1, 8, 2, 8])
    8
    >>> most_common([3, 5, 7, 7, 7, 5, 5])
    5
    >>> most_common([3, 7, 5, 5, 7, 7])
    7
    """
```

Implement the SparseList class. A SparseList instance represents a non-empty list s.

- Its common attribute is the most common value in s.
- Its others dictionary has a value for every element in s that is not common. The corresponding key is the index for that value in s.
- Its item method takes a non-negative integer i and returns s[i] or the string 'out of range' if i is not smaller than the length of s.
- Its items method returns a list with the same elements as s in the same order as s.

```
class SparseList:
```

"""Represent a non-empty list as a most common value and a dictionary from indices to values that contains only values that are not the most common.

```
>>> pi = SparseList([3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5])
>>> pi.common
5
>>> pi.others
\{0: 3, 1: 1, 2: 4, 3: 1, 5: 9, 6: 2, 7: 6, 9: 3\}
>>> [pi.item(0), pi.item(1), pi.item(2), pi.item(3), pi.item(4)]
[3, 1, 4, 1, 5]
>>> pi.item(10)
5
>>> pi.item(11)
'out of range'
>>> pi.items()
[3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5]
.....
def __init__(self, s):
    . . .
def item(self, i):
    . . .
def items(self):
    . . .
```

```
(a) (5.0 points)
```

Implement the __init__ method, which takes a list s.

```
def __init__(self, s):
  assert s, 's cannot be empty'
  self.n = len(s)
  self.common = most_common(_____)
                   (a)
```

- **i.** (1.0 pt) Fill in blank (a).
- ii. (1.0 pt) Which of these could fill in blank (b)?
 - () i 🔘 self.i \bigcirc n O self.n ○ s[i]
 - \bigcirc s
- iii. (1.0 pt) Fill in blank (c).

iv. (1.0 pt) Which of these could fill in blank (d)? Check all that apply.

🗌 s

- \Box len(s)
- □ self.s
- len(self.s)
- 🗌 n
- len(n)
- □ self.n
- len(self.n)
- **v.** (1.0 pt) Fill in blank (e).

(b) (3.0 points)

Implement the item method, which takes a non-negative integer i.

```
def item(self, i):
    """Return s[i] or 'out of range' if i is not smaller than the length of s."""
    assert i >= 0, 'index i must be non-negative'
    if ______:
        (a)
        return 'out of range'
    elif ______:
        (b)
        return ______(c)
```

else:

return self.common

- **i.** (1.0 pt) Fill in blank (a).
- **ii.** (1.0 pt) Fill in blank (b).

iii. (1.0 pt) Which of these could fill in blank (c)?

- others[i]
- O self.others[i]
- others[self.i]
- self.others[self.i]
- \bigcirc others
- \bigcirc self.others

(c) (4.0 points)

Implement the items method.

def items(self):

"""Return a list with the same elements as s in the same order as s."""

return [_____ for i in ____]
(a) (b)

i. (2.0 pt) Fill in blank (a). You may not use and, or, if, else, [,], or get.

Hint: Don't repeat yourself.

ii. (2.0 pt) Fill in blank (b).

4. (20.0 points) Fork It

The *tree* data abstraction, which is implemented by the constructor **tree**, selectors **branches** and **label**, and helper functions **is_leaf** and **is_tree** appear on Page 2 (left column) of the Midterm 2 Study Guide. You may call these functions. Do not violate the abstraction barriers of the tree data abstraction.

(a) (4.0 points)

Implement max_path, which takes a tree t whose labels are all positive numbers and returns the largest sum of the labels along a path from the root of t to one of its leaves.

You may call tree, label, branches, is_leaf, is_tree, and max_path.

```
def max_path(t):
    ""Return the largest sum of labels along any path from the root to a leaf
    of tree t, which has positive numbers as labels.
    >>> a = tree(1, [tree(2), tree(3), tree(4, [tree(5)])])
    >>> max_path(a) # 1 + 4 + 5
    10
    >>> b = tree(6, [a, a, a])
    >>> max_path(b) # 6 + 1 + 4 + 5
    16
    .....
    return _____ + max(_____ + ____)
(a) (b) (c)
 i. (1.0 pt) Which of the following could fill in blank (a)?
    \bigcirc t
    \bigcirc label(t)
    () [t]
    \bigcirc [label(t)]
    0 [0]

    sum([b for b in branches(t)])

    Sum([label(b) for b in branches(t)])
ii. (1.0 pt) Which of the following could fill in blank (b)?
    \bigcirc t
    \bigcirc label(t)
    () [t]
    \bigcirc [label(t)]
    0 [0]
```

 \bigcirc [label(b) for b in branches(t)]

iii. (2.0 pt) Fill in blank (c). You may not use the word default.

(b) (8.0 points)

Definition. A *fork* is a tree in which **exactly one node** has more than one child.





Implement is_fork and its helper function slide. The is_fork function takes a *tree* t and returns True if t is a fork and False otherwise.

You may call tree, label, branches, is_leaf, is_tree, max_path, is_fork, and slide.

```
def is_fork(t):
    """Return whether tree t is a fork.
    >>> is_fork(tree(1, [tree(2, [tree(3), tree(4), tree(5)])]))
    True
    >>> is_fork(tree(1, [tree(2, [tree(3)]), tree(4)]))
    True
    >>> is_fork(tree(1, [tree(2), tree(3), tree(4)]))
    True
    >>> is_fork(tree(1, [tree(2, [tree(3, [tree(5)]), tree(4, [tree(6)])]))))
    True
    >>> is_fork(tree(1), [tree(2, [tree(3)])], tree(4, [tree(6)])])))
    True
    >>> is_fork(tree(1), [tree(2, [tree(3)])])
    True
    >>> is_fork(tree(1), [tree(2, [tree(3)])])
```

```
>>> is_fork(tree(1, [tree(2, [tree(3)]), tree(4, [tree(5), tree(6)])]))
   False
   >>> is_fork(tree(1, [tree(2, [tree(3, [tree(5, [tree(7), tree(8)]), tree(6)]), tree(4)])]))
   False
    .....
   neck = slide(t)
   if is_leaf(neck):
        _____
           (a)
   return _____([_____ for b in branches(_____)])
(b) (c) (d)
def slide(t):
    """Return the deepest node within tree t whose ancestors all have exactly one child.
   Definition: The ancestors of a node include its parent and the parents of all its ancestors.
   >>> deepest = slide(tree(1, [tree(2, [tree(3)])]))
   >>> label(deepest)
   3
   >>> label(slide(tree(1, [tree(2, [tree(3), tree(4)])])))
   2
    .....
    while _____:
            (e)
        t = _____
               (f)
   return t
 i. (1.0 pt) Fill in blank (a).
```

ii. (1.0 pt) Which of the following could fill in blank (b)?

```
\bigcirc all
```

- \bigcirc any
- \bigcirc list
- \bigcirc tree
- \bigcirc branches
- \bigcirc label

iii. (2.0 pt) Fill in blank (c).

iv. (1.0 pt) Which of the following could fill in blank (d)?

- \bigcirc t
- \bigcirc tree
- \bigcirc neck
- \bigcirc label(t)
- () label(tree)
- \bigcirc label(neck)

v. (1.0 pt) Which of the following could fill in blank (e)?

- \bigcirc len(branches(t)) == 1
- \bigcirc len(branches(t)) > 1
- \bigcirc len(branches(t)) != 1
- \bigcirc branches(t) == 1
- \bigcirc branches(t) > 1
- \bigcirc branches(t) != 1
- **vi.** (2.0 pt) Fill in blank (f).

(c) (8.0 points)

Definition. A tree t *contains* a fork u if u is the result of pruning zero or more nodes from t.



Implement max_fork, which takes a tree t whose labels are all positive integers. It returns the largest sum of the labels of a fork that is contained in t. If t does not contain any forks, then max_fork returns 0.

You may call tree, label, branches, is_leaf, is_tree, max_path, is_fork, slide, and max_fork.

```
def max_fork(t):
```

"""Return the largest sum of the labels in any fork contained in tree t, which has positive numbers as labels. If t contains no forks, return 0.

```
>>> a = tree(1, [tree(2), tree(3), tree(4, [tree(5)])])
>>> max_fork(a) # 1 + 2 + 3 + 4 + 5
15
>>> b = tree(6, [a, a, a])
                            6 + (1 + 4 + 5) + (1 + 4 + 5) + (1 + 4 + 5)
>>> max_fork(b) #
36
>>> c = tree(7, [tree(8), b, tree(9)])
                     7 + (6 + (1 + 4 + 5) + (1 + 4 + 5) + (1 + 4 + 5))
>>> max_fork(c) #
43
>>> d = tree(9, [c])
>>> max_fork(d) \# 9 + 7 + (6 + (1 + 4 + 5) + (1 + 4 + 5) + (1 + 4 + 5))
52
>>> max_fork(tree(1, [tree(2, [tree(3)])])) # No forks here!
0
.....
n = len(branches(t))
if n == 0:
    return 0
elif n == 1:
    below = _____
               (a)
    if _____:
          (b)
```

else:

return 0

else:

return label(t) + max(here, there)

i. (2.0 pt) Fill in blank (a).

ii. (1.0 pt) Which of the these could fill in blank (b)?

```
> below > 0
> label(t) > 0
> max_fork(t) > 0
True
max_fork(t) > max_path(t)
is_fork(t)
```

iii. (1.0 pt) Which of these could fill in blank (c)?

- 01
- \bigcirc label(t)
- \bigcirc max_path(t)
- () label(slide(t))
- max([label(b) for b in branches(t)])
- \bigcirc label(branches(t)[0])

iv. (2.0 pt) Fill in blank (d).

v. (2.0 pt) Fill in blank (e).

No more questions.