

The result of calling `repr` on a value is what Python displays in an interactive session

```
>>> today = datetime.date(2019, 10, 13)
>>> repr(today) # or today.__repr__()
'datetime.date(2019, 10, 13)'
>>> str(today) # or today.__str__()
'2019-10-13'
```

The result of evaluating an f-string literal contains the str string of the value of each sub-expression.

```
>>> f'pi starts with {pi}...'
'pi starts with 3.141592653589793...'
>>> print(f'pi starts with {pi}...')
pi starts with 3.141592653589793...
```

Lists:

```
>>> digits = [1, 8, 2, 8]
>>> len(digits)
4
>>> digits[3]  digits |---> list
4
[0 1 2 3]
1 8 2 8
```

```
>>> [2, 7] + digits * 2
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
```

```
>>> pairs = [[10, 20], [30, 40]]
>>> pairs[1]  pairs |---> list
[0 1]
10 20
```

Executing a for statement:

```
for <name> in <expression>:
    <suite>
```

- Evaluate the header `<expression>`, which must yield an iterable value (a list, tuple, iterator, etc.)
- For each element in that sequence, in order:
 - Bind `<name>` to that element in the current frame
 - Execute the `<suite>`

Unpacking in a for statement:

```
A sequence of
fixed-length sequences
```

```
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
>>> same_count = 0
```

A name for each element in a fixed-length sequence

```
>>> for x, y in pairs:
...     if x == y:
...         same_count = same_count + 1
>>> same_count
2
```

```
..., -3, -2, -1, 0, 1, 2, 3, 4, ...
range(-2, 2)
```

Length: ending value – starting value

Element selection: starting value + index

```
>>> list(range(-2, 2))  List constructor
[-2, -1, 0, 1]
```

```
>>> list(range(4))  Range with a 0
[0, 1, 2, 3] starting value
```

Membership:

```
>>> digits = [1, 8, 2, 8]
>>> 2 in digits
True
```

```
>>> 1828 not in digits
True
```

Slicing creates a new object

Identity:

`<exp0> is <exp1>`

evaluates to `True` if both `<exp0>` and `<exp1>` evaluate to the same object

Equality:

`<exp0> == <exp1>`

evaluates to `True` if both `<exp0>` and `<exp1>` evaluate to equal values

Identical objects are always equal values

```
iter(iterator):
    Return an iterator
    over the elements of
    an iterable value
next(iterator):
    Return the next element
```

`>>> s = [3, 4, 5] d = {'one': 1, 'two': 2, 'three': 3}`

`>>> t = iter(s) k = iter(d) v = iter(d.values())`

`>>> next(t) >>> next(k) >>> next(v)`

`>>> next(t) >>> next(k) >>> next(v)`

`>>> next(t) >>> next(k) >>> next(v)`

A generator function is a function that `yields` values instead of `returning`.

```
>>> def plus_minus(x): >>> t = plus_minus(3)  def a_then_b(a, b):
...     yield x  >>> next(t)  >>> a_then_b([3, 4], [5, 6])
...     yield -x  3  >>> list(a_then_b([3, 4], [5, 6]))
```

`>>> next(t) >>> next(t) >>> list(a_then_b([3, 4], [5, 6]))`

`-3 3, 4, 5, 6`

List comprehensions:

[`<map exp> for <name> in <iter exp> if <filter exp>`]

Short version: [`<map exp> for <name> in <iter exp>`]

A combined expression that evaluates to a list using this evaluation procedure:

- Add a new frame with the current frame as its parent
- Create an empty `result list` that is the value of the expression
- For each element in the iterable value of `<iter exp>`:
 - Bind `<name>` to that element in the new frame from step 1
 - If `<filter exp>` evaluates to a true value, then add the value of `<map exp>` to the result list

Dictionaries:

```
words = {
    "más": "more",
    "otro": "other",
    "agua": "water"
}
```

`>>> len(words)`

3

"agua" in words

True

words["otro"]

'other'

words["pavo"]

KeyError

words.get("pavo", "调理")

'调理'

words["oruguita"]

'caterpillar'

words["oruguita"] += '调理'

'caterpillar调理'

Dictionary comprehensions:

{key: value for <name> in <iter exp>}

```
>>> {x: x*x for x in range(3,6)}
{3: 9, 4: 16, 5: 25}
```

Functions that aggregate iterable arguments

- | | | |
|--|--|-----------------------------------|
| <code>>>> sum([1, 2])</code> | <code>>>> sum([1, 2])</code> | <code>sum of all values</code> |
| <code>>>> max([1, 2])</code> | <code>>>> max([1, 2])</code> | <code>largest value</code> |
| <code>>>> min([1, 2])</code> | <code>>>> min([1, 2])</code> | <code>smallest value</code> |
| <code>>>> all([True, False])</code> | <code>>>> all([True, False])</code> | <code>whether all are true</code> |
| <code>>>> any([False, True])</code> | <code>>>> any([False, True])</code> | <code>whether any is true</code> |

Many built-in Python sequence operations return iterators that compute results lazily

To view the contents of an iterator, place the resulting elements into a container

```
def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)
        cascade(n//10)
        print(n)
```

`map(func, iterable):`
Iterate over `func(x)` for `x` in iterable

`filter(func, iterable):`
Iterate over `x` in iterable if `func(x)`

`zip(first_iter, second_iter):`
Iterate over co-indexed (`x, y`) pairs

`reversed(sequence):`
Iterate over `x` in a sequence in reverse order

`list(iterator):`
Create a list containing all `x` in iterable

`tuple(iterator):`
Create a tuple containing all `x` in iterable

`sorted(iterator):`
Create a sorted list containing `x` in iterable

```
def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)
        cascade(n//10)
        print(n)

def virfib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return virfib(n-2) + virfib(n-1)
```

`n: 0, 1, 2, 3, 4, 5, 6, 7, 8,`

`virfib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,`

Exponential growth. E.g., recursive fib

Incrementing `n` multiplies time by a constant

Quadratic growth. E.g., overlap

Incrementing `n` increases time by `n` times a constant

Linear growth. E.g., slow exp

Incrementing `n` increases time by a constant

Logarithmic growth. E.g., exp_fast

Doubling `n` only increments time by a constant

Constant growth. Increasing `n` doesn't affect time

$\Theta(b^n)$ $O(b^n)$

$\Theta(n^2)$ $O(n^2)$

$\Theta(n)$ $O(n)$

$\Theta(\log n)$ $O(\log n)$

$\Theta(1)$ $O(1)$



Global frame

`make_withdraw_list`

`withdraw`

`balance`

`b`

`Return value`

`f1: make_withdraw_list [parent=Global]`

`withdraw`

`balance`

`b`

`Return value`

`f2: withdraw [parent=f1]`

`amount`

`b`

`Return value`

List mutation:

```
>>> a = [10]  >>> a = [10]
>>> b = a  >>> b = [10]
>>> a == b  >>> a == b
True  True
True
>>> a.append(20)  >>> b.append(20)
>>> a == b  >>> a == b
[10, 20]  [10, 20]
>>> b  >>> b
[10, 20]  [10, 20]
False
```

You can `copy` a list by calling the list constructor or slicing the list from the beginning to the end.

`>>> a = [10, 20, 30]`

`>>> list(a)`

`[10, 20, 30]`

`>>> a[:]`

`[10, 20, 30]`

`>>> a`

`[10, 20, 30]`

`>>> b`

`[10, 20]`

`>>> a == b`

`False`

Tuples:

`>>> empty = ()`

`>>> len(empty)`

`0`

`>>> conditions = ('rain', 'shine')`

`>>> conditions[0]`

`'rain'`

`>>> conditions[0] = 'fog'`

`Error`

False values:

`>>> bool(0)`

`False`

`>>> bool(1)`

`True`

`>>> bool('')`

`False`

`>>> bool('0')`

`True`

`>>> bool([])`

`False`

`>>> bool({})`

`False`

`>>> bool(())`

`False`

`>>> bool(lambda x: 0)`

`True`

`>>> bool(None)`

`False`

`>>> bool(False)`

`False`

`>>> bool(True)`

`True`

`>>> bool(1)`

`True`

`>>> bool('1')`

`True`

`>>> bool('10')`

`True`

`>>> bool([1, 2])`

`True`

`>>> bool([1, 2, 3])`

`True`

`>>> bool([1, 2, 3, 4])`

`True`

`>>> bool([1, 2, 3, 4, 5])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19])`

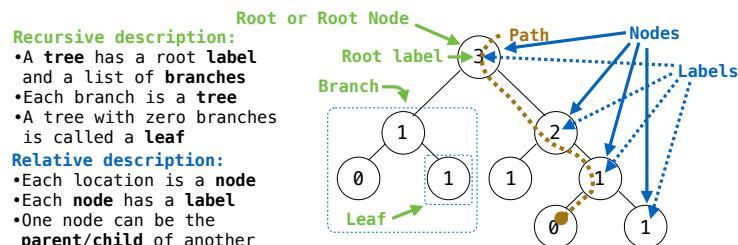
`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20])`

`True`

`>>> bool([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21])`

`True`



- Each location is a **node**
- Each **node** has a **label**
- One node can be the **parent/child** of another

```

def tree(label, branches=[]):
    for branch in branches:
        assert is_tree(branch)
    return [label] + list(branches)

def label(tree):
    return tree[0]

def branches(tree):
    return tree[1:]

def is_tree(tree):
    if type(tree) != list or len(tree) < 1:
        return False
    for branch in branches(tree):
        if not is_tree(branch):
            return False
    return True

def is_leaf(tree):
    return not branches(tree)

def leaves(t):
    """The leaf values in t.
    >>> leaves(fib_tree(5))
    [1, 0, 1, 0, 1, 1, 0, 1]
    """
    if is_leaf(t):
        return [label(t)]
    else:
        return sum([leaves(b) for b in branches(t)], [])

def fib_tree(n):
    if n == 0 or n == 1:
        return tree(n)
    else:
        left = fib_tree(n-2),
        right = fib_tree(n-1)
        fib_n = label(left) + label(right)
        return tree(fib_n, [left, right])

```

```

>>> tree(3, [tree(1), tree(2, [tree(1), tree(1)])])
[3, [1], [2, [1], [1]]]

```

```
class Tree:  
    def __init__(self, label, branches=[]):  
        self.label = label  
        for branch in branches:  
            assert isinstance(branch, Tree)  
        self.branches = list(branches)
```

Built-in `isinstance` function: returns True if `branch` has a class that *is* or *inherits from* `Tree`

```
def is_leaf(self):
    return not self.branches
>>> b = Tree(2, [Tree(3)])
>>> t = Tree(1, [b, Tree(4)])
```



```
def fib_tree(n):
    if n == 0 or n == 1:
        return Tree(n)
    else:
        left = fib_tree(n-2)
```

```
>>> t
Tree(1, [Tree(2, [Tree(3)]), Tree(4)])
>>> print(t)
1
  2
    3
    4
  2   4
    3
      1
```

```

class Link:
    empty = ()  
    Some zero  
    length sequence

    def __init__(self, first, rest=empty):
        self.first = first
        self.rest = rest

    def __repr__(self):
        if self.rest:
            rest = ', ' + repr(self.rest)
        else:
            rest = ''
        return 'Link(' + repr(self.first) + rest + ')'

    def __str__(self):
        string = '<'
        while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + '>'

    def __eq__(self, other):
        if type(self) != type(other):
            return False
        if self.empty == other.empty:
            return True
        if len(self) != len(other):
            return False
        for first, other_first in zip(self, other):
            if first != other_first:
                return False
        return True

```

Link instance Link instance

first:	4	first:	5
rest:		rest:	

```

>>> s = Link(4, Link(5))
>>> s
Link(4, Link(5))
>>> s.first
4
>>> s.rest
Link(5)
>>> print(s)
<4 5>
>>> print(s.rest)
<5>
>>> s.rest.rest is Link.empty
True

```

The **def statement header** is like any function
Conditional statements check for **base cases**
Base cases are evaluated **without recursive calls**
Recursive cases are evaluated **with recursive calls**

```
def sum_digits(n):
    "Sum the digits of positive integer n."
    if n < 10:
        return n
    else:
```

```
Recursive decomposition: finding simpler instances of a problem.  
E.g., count_partitions(6, 4)  
Explore two possibilities:  
  Use at least one 4  
  Don't use any 4  
Solve two simpler problems:  
  count_partitions(2, 4)  
  count_partitions(6, 3)  
Tree recursion often involves exploring different choices.  
  
def count_partitions(n, m):  
    if n == 0:  
        return 1  
    elif n < 0:  
        return 0  
    elif m == 0:  
        return 0  
    else:  
        with_m = count_partitions(n-m, m)  
        without_m = count_partitions(n, m-1)  
        return with_m + without_m
```

Python object system

Idea: All bank accounts have a `balance` and an account `holder`; the `Account` class should add those attributes to each of its instances

A new instance is created by calling a class

```
>>> a = Account('Jim')
>>> a.holder
'Jim'
>>> a.balance
```

When a class is called:

- 1.A new instance of that class is created: balance: 0 holder: 'Jim'
2.The `__init__` method of the class is called with the new object as its first argument (named `self`), along with any additional arguments provided in the call expression.

```
class Account:  
    def __init__(self, account_holder):  
        self.balance = 0  
        self.holder = account_holder
```

self should always be bound to an instance of the Account class or a subclass of Account

Function call: all arguments within parentheses

Method invocation: One object before the dot and other arguments within parentheses

For more information about the study, please contact the study team at 1-800-258-4929 or visit www.cancer.gov.

<expressions>

The `<expression>` can be any valid Python expression.
The `<name>` must be a simple name.
Evaluates to the value of the attribute looked up by `__getattr__` in the object.

evaluates to the value of the attribute looked up by `<name>` in the object that is the value of the `<expression>`.

To evaluate a dot expression:

1. Evaluate the `<expression>` to the left of the dot, which yields the object of the dot expression
2. `<name>` is matched against the instance attributes of that object. If an attribute with that name exists, its value is returned.
3. If not, `<name>` is looked up in the class, which yields a class attribute value.
4. That value is returned unless it is a function, in which case a bound method is returned instead.

Assignment statements with a dot expression on their left-hand side affect attributes for the object of that dot expression

- If the object is an instance, then assignment sets an instance attribute
 - If the object is a class, then assignment sets a class attribute

Account class
attributes

```
Instance attributes of jim_account    balance: 0
                                         holder: 'Jim'
                                         interest: 0.08
                                         Instance attributes of tom_account    balance: 0
                                         holder: 'Tom'
```

```
>>> jim_account = Account('Jim')
>>> tom_account = Account('Tom')
>>> tom_account.interest
0.02
>>> jim_account.interest
0.02
>>> Account.interest = 0.04
>>> tom_account.interest
0.04
>>> jim_account.interest
0.04
>>> jim_account.interest = 0.08
>>> jim_account.interest
0.08
>>> tom_account.interest
0.04
>>> Account.interest = 0.05
>>> tom_account.interest
0.05
>>> jim_account.interest
0.08
```

```
class CheckingAccount(Account):
    """A bank account that charges for withdrawals."""
    ...
```

```
withdraw_fee = 1  
interest = 0.01
```

```
def withdraw(self, amount):
    return Account.withdraw(self, amount + self.withdraw_fee)
```

To look up a name in a class:
1. If it names an attribute in the class, return the attribute.
2. Otherwise, look up the name in the base class, if there is one.

To look up a name in a class:

1. If it names an attribute in the class, return the attribute value.
2. Otherwise, look up the name in the base class, if there is one.

```
>>> ch = CheckingAccount('Tom') # Calls Account.__init__
>>> ch.interest      # Found in CheckingAccount
0.01
>>> ch.deposit(20)   # Found in Account
20
>>> ch.withdraw(5)   # Found in CheckingAccount
15
```