

Import statement

```
1 from math import pi
2 tau = 2 * pi
```

Assignment statement

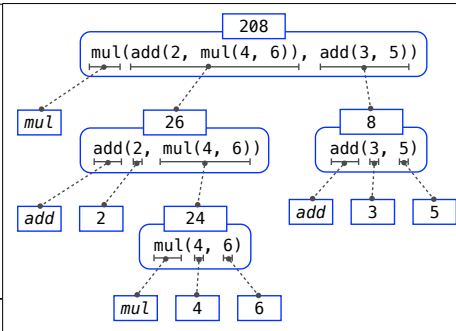
Global frame

Name	Value
pi	3.1416

Binding

Code (left): Statements and expressions
Red arrow points to next line. Gray arrow points to the line just executed

Frames (right): A name is bound to a value
In a frame, there is at most one binding per name



Pure Functions

```
-2 abs(number): 2
2, 10 pow(x, y): 1024
```

Non-Pure Functions

```
-2 print(...): None
```

display "-2"

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(-2)
```

Global frame

Name	Value
mul	mul
square	func square(x) [parent=Global]

Intrinsic name of function called

Local frame

Name	Value
f1: square	[parent=Global]
x	-2
Return value	4

Formal parameter bound to argument

Return value is not a binding!

Built-in function

User-defined function

Defining:

```
>>> def square(x):
    return mul(x, x)
```

Def statement

Formal parameter: x

Return expression: mul(x, x)

Body (return statement): return mul(x, x)

Call expression: square(2+2)

operator: square
function: func square(x)

operand: 2+2
argument: 4

```
1 def strconcat(a, b):
2     print(a + " " + b)
3
4 strconcat("hello", "world")
```

hello world

A and B:
True if A is True and B is True
A or B:
True if A is True or B is True
not A:
True if A is False
False if A is True

def abs_value(x):

```
1 statement,
2 clauses,
3 headers,
3 suites,
2 boolean contexts
```

```
if x > 0:
    return x
elif x == 0:
    return 0
else:
    return -x
```

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(square(3))
```

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

Global frame

Name	Value
mul	mul
square	func square(x) [parent=Global]

Local frame

Name	Value
f1: square	[parent=Global]
x	3
Return value	9

Local frame

Name	Value
f2: square	[parent=Global]
x	9
Return value	81

Calling/Applying: square(x)

Argument: x

Intrinsic name: square

Return value: mul(x, x)

def f(x, y):

```
1 def f(x, y):
2     return g(x)
3
4 def g(a):
5     return a + y
6
7 result = f(1, 2)
```

Global frame

Name	Value
f	func f(x, y) [parent=Global]
g	func g(a) [parent=Global]

Local frame

Name	Value
f1: f	[parent=Global]
x	1
y	2

Local frame

Name	Value
f2: g	[parent=Global]
a	1

Error: "y" is not found

- An environment is a sequence of frames
- An environment for a non-nested function (no def within def) consists of one local frame, followed by the global frame

Evaluation rule for call expressions:

- Evaluate the operator and operand subexpressions.
- Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

Applying user-defined functions:

- Create a new local frame with the same parent as the function that was applied.
- Bind the arguments to the function's formal parameter names in that frame.
- Execute the body of the function in the environment beginning at that frame.

Execution rule for def statements:

- Create a new function value with the specified name, formal parameters, and function body.
- Its parent is the first frame of the current environment.
- Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

- Evaluate the expression(s) on the right of the equal sign.
- Simultaneously bind the names on the left to those values, in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order.

- Evaluate the header's expression.
- If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- Evaluate the subexpression <left>.
- If the result is a true value v, then the expression evaluates to v.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

- Evaluate the subexpression <left>.
- If the result is a false value v, then the expression evaluates to v.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

- Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

- Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.

Higher-order function: A function that takes a function as an argument value or returns a function as a return value

Nested def statements: Functions defined within other function bodies are bound to names in the local frame

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(4)
```

Global frame

Name	Value
mul	mul
square	func square(x) [parent=Global]

Local frame

Name	Value
f1: square	[parent=Global]
x	4
Return value	16

A call expression and the body of the function being called are evaluated in different environments

```
def fib(n):
    """Compute the nth Fibonacci number, for N >= 1."""
    pred, curr = 0, 1 # Zeroth and first Fibonacci numbers
    k = 1 # curr is the kth Fibonacci number
    while k < n:
        pred, curr = curr, pred + curr
        k = k + 1
    return curr
```

def cube(k):

```
return pow(k, 3)
```

Function of a single argument (not called term)

def summation(n, term):

```
"""Sum the first n terms of a sequence."""
```

A formal parameter that will be bound to a function

```
>>> summation(5, cube)
225
"""
total, k = 0, 1
while k <= n:
    total, k = total + term(k), k + 1
return total
0 + 1^3 + 2^3 + 3^3 + 4^3 + 5^3
```

The cube function is passed as an argument value

The function bound to term gets called here

def cube(k):

```
return pow(k, 3)
```

Function of a single argument (not called term)

def summation(n, term):

```
"""Sum the first n terms of a sequence."""
```

A formal parameter that will be bound to a function

Higher-order function: A function that takes a function as an argument value or returns a function as a return value

Nested def statements: Functions defined within other function bodies are bound to names in the local frame

